³¹P Solid-state NMR Spectra of Crystalline Phosphoric Acid and their Relation to the Structure of Urea Phosphate

Alejandro J. Vila, a Claudia M. Lagier, b George Wagner and Alejandro C. Olivieri* a,b

 IQUIOS, Facultad de Ciencias Bioquimicas y Farmaceuticas, SuipACHA 531, Rosario 2000, Argentina
 Departamento de Quimica Analitica, Facultad de Ciencias Bioquimicas Farmaceuticas, Suipacha 531, Rosario 2000, Argentina

^c Molecular Spectroscopy Laboratory, Department of Chemistry, University of Illinois at Urbana-Champaign, Urbana, IL 61801, USA

The ³¹P chemical shift tensor in crystalline phosphoric acid at 123 K is axially symmetric, with $\Delta \sigma = +60$ ppm; at room temperature a very small $\Delta \sigma$ is observed, indicating either fast reorientational motion of PO₄ tetrahedra or multiple proton transfer.

The relation between ³¹P NMR chemical shift data and structural factors has been noted.^{1–7} In addition to the isotropic information commonly recorded in solution, solid-state NMR data provide important tensorial values which depend on the spatial distribution of electron density at the

phosphorus atom. When all four ligands are oxygens and non-nearest ligand effects are neglected, the chemical shift anisotropy, $\Delta\sigma$, seems to be sensitive to P–O bond lengths and angles.^{4–7} Various forms of empirical correlation have been attempted.^{4–6} Recently, a semiempirical model based on a



	$\sigma_{jj} = \sigma_1$					
Compound	<i>j</i> = 1	<i>j</i> = 2	<i>j</i> = 3	$\Delta \sigma$	σ_1	Ref.
NaH ₂ PO ₄ ·H ₂ O	-58.8	-20.8	79.6	119.4	-2.3	5
$Ca(H_2PO_4)_2 \cdot H_2O$	-59.0 -49.0	-7.0	$66.0 \\ 49.0$	99.0 73.5	0.0 -0.7	10 10
UPA H₃PO₄ at 123 K	-31.8 -20	-7.6 -20	39.4 40	59.1 60	5.2 0.9	8 b

^{*a*} All values are in ppm from 85% aqueous phosphoric acid. ^{*b*} This work.



Fig. 3 Plot of the principal values of the tensor $<\Delta\sigma>$ as a function of *p*. Experimental points (see Table 1) are indicated as circles.

between a hydrogen bonded adduct and a uronium salt.8,9 Reported values for the chemical shift tensor (CST) in UPA differ from those measured for dihydrogen phosphate species (Table 1), not only in magnitude but also in orientation in the molecular frame.8 In order to study the relation between CST in H₂PO₄⁻, H₃PO₄ and UPA, we recorded the ³¹P solid-state NMR spectrum of H₃PO₄. At room temperature, a line showing very small $\Delta \sigma$ is obtained (Fig. 1). This result was not the expected one on the basis of the diffraction data reported in the literature.^{11,12} Therefore, low temperature spectra were acquired. At 123 K (Fig. 1) a considerably larger $\Delta\sigma$ (+60 ppm, with positive values indicating increasing shielding) is apparent, corresponding to an axially symmetric CST. The changes observed with increasing temperatures may be due to averaging processes including: (a) molecular motions faster than the width of $\Delta\sigma$ (ca. 7 kHz) or (b) multiple proton transfer among nearby molecules. These variable-temperature results will be described elsewhere.

We take the 123 K ³¹P CST as representative of static H₃PO₄ molecules in crystals. Accurate values of P-O bond lengths in this case are available from low temperature neutron diffraction data for H₃PO₄ itself [short bond (SB), 1.496 Å; average of long bonds (LB), 1.546 Å]¹¹ and from the adduct H₃PO₄·CH₃COOH, in which H₃PO₄ is unionized (1.489 and 1.540 Å respectively).¹² The above mentioned model involving the calculation of P–O π bond orders led to the relation $\Delta \sigma = +290$ ppm ($\pi_{SB} - \pi_{LB}$) for (RO)₃PO species.⁷ Hence, $\Delta \sigma$ is predicted to be +65 ppm, close to the experimental value. Using the orientation of the principal axes of the CST in $H_3PO_4(a)$ and $H_2PO_4^-(b)$ in the xyz frame of Fig. 2, the anisotropic part of the CST in UPA will be given by $\langle \Delta \sigma \rangle = p \Delta \sigma_b + (1 - p) \Delta \sigma_a$. The CST at site *b* is diagonal in the xyz frame, whereas in the case of site $a \sigma \perp$ points along the z axis, but the other components are offset from the x and yaxes. After matrix rotation in the xy plane, nonvanishing offdiagonal components are created in the xy plane, giving the following final result:



Fig. 1 ³¹P Solid-state NMR spectra of crystalline phosphoric acid. (*a*) At room temperature (296 K) and (*b*) at 123 K. Both spectra were recorded on a General Electric GN300WB spectrometer operating at 121.5 MHz. The conventional one pulse sequence was used, with proton decoupling during acquisition. Spectral parameters: ³¹P pulse width, (*a*) 8.8 μ s, (*b*) 10.0 μ s; recycle delay, (*a*) 10.5 s; number of transients, (*a*) 64, (*b*) 264; spectral width, 40 kHz; acquisition time, 51.2 ms; 4 K memory; spinning rate, (*a*) 1.3 kHz; (*b*) 2.7 kHz. Both scales are in ppm from 85% aqueous H₃PO₄, with positive values indicating increasing shielding. Low temperature was achieved by cooling the N₂ driving the rotor in liquid nitrogen. CST information was retrieved using the method described by Herzfeld and Berger¹³ from data in spectrum (*b*) and other slow spinning spectra at the same temperature.



Fig. 2 Assumed orientation for the principal axes of the CST in H_3PO_4 (left) and $H_2PO_4^-$ (right)

combination of four axially symmetric P–O bond tensors⁷ has been qualitatively applied to urea phosphate (UPA), where phosphoric acid undergoes proton transfer to a urea molecule, giving a structure with geometrical features which are midway

$$<\Delta\sigma>= \begin{vmatrix} p(\sigma_{33} - \sigma_{i}) + (1 - p)\Delta\sigma/3 & -\sqrt{2}(1 - p)\Delta\sigma/3 & 0\\ -\sqrt{2}(1 - p)\Delta\sigma/3 & p(\sigma_{22} - \sigma_{i}) & 0\\ 0 & 0 & p(\sigma_{11} - \sigma_{i}) - (1 - p)\Delta\sigma/3 \end{vmatrix}$$

where $\sigma_{ij} - \sigma_i$ (j = 1, 2, 3) correspond to H₂PO₄⁻, $\Delta \sigma$ to H₃PO₄ and p is the degree of proton transfer. Inserting $p = 0.5,^9 \Delta \sigma$ from the present measurements and $\sigma_{jj} - \sigma_i$ as the average of the values given in Table 1, the principal values of $\langle \Delta \sigma \rangle$ are -37.8, -8.6 and +46.3, in good agreement with the experimental ones. Further illustration of this point is given in Fig. 3, where the components of $<\Delta\sigma>$ are plotted as a function of p, and experimental points are quoted. In conclusion, CST values measured at 123 K correlate well with the crystal structure of H₃PO₄, since only in this case is the reorientational motion present at room temperature in the slow regime.

We acknowledge financial support from CONICET (Consejo Nacional de Investigaciones Científicas y Tecnicas), the University of Rosario, the Fundacion Antorchas (RG No. 11842) and TWAS (Third World Academy of Sciences, RG No. BC 890-060). A. J. V. thanks CONICET for a fellowship.

Received, 14th August 1990; Com. 0/03737K

$$\begin{array}{cccc}
2(1-p)\Delta\sigma/3 & 0 \\
p(\sigma_{22} - \sigma_{i}) & 0 \\
0 & p(\sigma_{11} - \sigma_{i}) - (1-p)\Delta\sigma/3
\end{array}$$

References

- 1 J. H. Lecher and J. R. Van Wazer, Top. Phosphorus Chem., 1967, 75; J. Chem. Phys., 1965, 44, 815.
- 2 D. G. Gorenstein, in Phosphorus-31 NMR, ed. D. G. Gorenstein, Academic Press, San Francisco, 1984, pp. 7-36.
- 3 F. R. Prado, C. Geissner-Prettre, B. Pullman and J. P. Daudey, J. Am. Chem. Soc., 1979, 101, 1737.
- 4 A. R. Grimmer, Spectrochim. Acta, 1978, 34A, 941.
 5 G. L. Turner, K. A. Smith, R. J. Kirkpatrick and E. Oldfield, J. Magn. Reson., 1986, 70, 408.
- 6 S. Un and M. P. Klein, J. Am. Chem. Soc., 1989, 111, 5119.
- 7 A. C. Olivieri, J. Magn. Reson., 1990, 88, 1.
- 8 J. Herzfeld, R. G. Griffin and R. A. Haberkorn, Biochemistry, 1978, 17, 2711.
- 9 D. Mootz and K. R. Albrand, Acta Crystallogr. Sect. B, 1972, 28, 2459.
- 10 W. P. Rothwell, J. S. Waugh and J. P. Yesinowski, J. Am. Chem. Soc., 1980, 102, 2637.
- 11 F. E. Cole, Ph. D. Diss., Washington State Univ., 1966.
- 12 P. G. Jönsson, Acta Chem. Scand., 1972, 26, 1599.
- 13 J. Herzfeld and A. E. Berger, J. Chem. Phys., 1980, 73, 6021.